

Problema săptămânii 69

Determinați cea mai mică valoare posibilă a expresiei

$$\frac{1}{a+x} + \frac{1}{a+y} + \frac{1}{b+x} + \frac{1}{b+y},$$

unde a, b, x și y sunt numere reale pozitive care satisfac inegalitățile:

$$\frac{1}{a+x} \geq \frac{1}{2}, \quad \frac{1}{a+y} \geq \frac{1}{2}, \quad \frac{1}{b+x} \geq \frac{1}{2} \quad \text{și} \quad \frac{1}{b+y} \geq 1.$$

Problem of the week no. 69

Determine the lowest possible value of the expression

$$\frac{1}{a+x} + \frac{1}{a+y} + \frac{1}{b+x} + \frac{1}{b+y}$$

where a, b, x , and y are positive real numbers satisfying the inequalities

$$\frac{1}{a+x} \geq \frac{1}{2}, \quad \frac{1}{a+y} \geq \frac{1}{2}, \quad \frac{1}{b+x} \geq \frac{1}{2}, \quad \text{and} \quad \frac{1}{b+y} \geq 1.$$