## "DIFFICULT-EASY PROBLEMS" FROM GEOMETRY

## Part 1

Problem 1. Suppose $A B C D$ is a rectangle where $A B=$ $B M=M N=N C$. What is the value of $\angle M A D+\angle N A D+$ $\angle C A D$ ?


Problem 2. Suppose $A B C D$ is a square, point $K$ is midpoint of side $A B$ while $M$ lies on diagonal $A C$, so that $A M: M C=3: 1$. Determine the value of $\angle K M D$.


Problem 3. A point $M$ is chosen inside a square $A B C D$ so that $\angle M A B=60^{\circ}$, while $\angle M C D=15^{\circ}$. Determine the value of $\angle M B C$.


Problem 4. A point $M$ is chosen inside a square $A B C D$ so that $\angle M A B=30^{\circ}$, while $\angle M C B=15^{\circ}$. Determine the value of $\angle M D A$.


Problem 5. A point $M$ is chosen inside a square $A B C D$ so that $B M: C M: D M=1: 2: 3$. Determine the value of $\angle B M C$.


Problem 6. $A B C$ is isosceles triangle with $\angle A=$ $\angle C=80^{\circ}$. Points $D$ and $E$ are marked on sides $A B$ and $B C$ respectively so that $\angle A D C=60^{\circ}$ and $\angle A E C=50^{\circ}$. Determine the value of $\angle D E A$.


Problem 7. Triangle $A B C$ is isosceles $(A B=B C)$ and $\angle A B C=80^{\circ}$. Point $P$ is marked in interior of $A B C$ so that $\angle A C P=30^{\circ}$ while $\angle P A C=40^{\circ}$. What is the value of $\angle B P C$ ?


Problem 8. Triangle $A B C$ is isosceles $(A B=B C)$ and $\angle A B C=80^{\circ}$. Point $P$ is marked in interior of $A B C$ so that $\angle P A C=30^{\circ}$ while $\angle P C A=10^{\circ}$. What is the value of $\angle B P C$ ?


Problem 9. Suppose that in triangle $A B C, A H$ is an altitude, $B E$ is bisector and $\angle A H E=45^{\circ}$. What is the value of $\angle E H C$ ?


Problem 10. Point $K$ is marked on side $B C$ of triangle $A B C$ so that $B K=2 K C$. Given that $\angle A C B=45^{\circ}, \angle A K B=60^{\circ}$. Determine the value of $\angle A B C$.


Problem 11. Suppose that in triangle $A B C, A A^{\prime}, B B^{\prime}$, and $C C^{\prime}$ are bisectors and $\angle A B C=120^{\circ}$.
(a) Determine the value of $\angle C^{\prime} B^{\prime} A^{\prime}$;

(b) Determine the value of $\angle B^{\prime} C^{\prime} C$.

